A Pure Characteristics Demand Model for Automobile Variants

Øyvind Thomassen *

This paper suggests a way to estimate a structural demand model for differentiated products using a single cross section of productlevel data. Bajari and Benkard (2005) use revealed-preference bounds for the taste coefficients. In order to obtain point estimates, I modify their model in two ways. First, I impose additional bounds on the willingness to pay for characteristics, based on the price consumers actually paid for the product they purchased. Secondly, I make an assumption about the distribution of taste coefficients within the bounds for each product. I estimate the model with data on new car sales in Norway.

Keywords: Discrete choice, Demand estimation, Differentiated products, Automobiles

JEL Classification: C35, D12, L62

I. Introduction

The aim of this paper is to demonstrate, via an empirical example, how to obtain point estimates of price elasticities in a differentiated products market using a single cross section of product-level data. I estimate the model using data on sales of new car model variants in Norway in 2004.

The paper estimates a structural model of the demand for automobiles based on Bajari and Benkard (2005). Their model produces bounds on price elasticities. In order to obtain point estimates of elasticities I modify their model by imposing weak and a priori reasonable bounds on con-

*Assistant Professor, Department of Economics, Seoul National University. Address: 599, Gwanakro, Silim 9-Dong, Gwanak-gu, Seoul 151-746, (Tel) +82-2-880-6376, (E-mail) oyvind.thomassen@gmail.com, Financial support from the Institute of Economic Research of Seoul National University is gratefully acknowledged.

[Seoul Journal of Economics 2014, Vol. 27, No. 2]

sumers' willingness to pay for a characteristic as a percentage of the price of the product they purchased. As in the random-coefficients logit literature (Berry, Levinsohn, and Pakes (1995); Nevo (2001)) utility is linear in product characteristics and tastes for characteristics have a distribution in the population of consumers. The main difference from this literature is that consumers do not have an idiosyncratic taste for products (like the logit term) that is unrelated to observable characteristics.

A first stage estimates a scalar unobservable product characteristic for each alternative. A second stage finds the sets of coefficients that can rationalise the choice of each product. Under utility maximisation, the choice of a given alternative implies that this alternative's utility is greater than those of all the other alternatives. These inequalities imply bounds on the combinations of taste coefficients a consumer could possibly have, given his choice. In principle, as the number of products goes to infinity, the sets of implied taste coefficients for each product should become singletons. However, in practice, only bounds for each alternative are implied by the data. Bajari and Benkard (2005) proceed to aggregate the bounds derived from individual choices to get bounds on the aggregate taste distributions.

Any product which has less of a given characteristic than the consumer's chosen product provides a lower bound on that consumer's taste for the characteristic (conditional on his tastes for the other characteristics). Vice versa, any product with more of the characteristic provides an upper bound on the consumer's taste. Some characteristics take on only a few discrete values, and in many cases only two: a 0 or 1. For instance a car either has automatic or manual transmission. For dummy (binary) variables we obtain either only lower bounds (if the chosen product has a 1) or only upper bounds (if 0). This means that the set of taste coefficients will not be bounded.

This problem can be mitigated by imposing conservative bounds on the distributions of tastes. I propose to use bounds on the willingnessto-pay for characteristics, expressed as a percentage of the price paid for the product actually chosen. This provides a way of choosing conservative bounds that are economically meaningful, and which vary with preferences.

The next section describes the Norwegian car market and the data used for estimation. The third section discusses relevant aspects of the literature, particularly the vertical differentiation model and issues relating to idiosyncratic taste shocks. The fourth section sets out the model and discusses identification. The fifth section explains the estimation procedure. The sixth section presents and discusses the results.

II. Background and Data

A. The Norwegian car market

This paper focuses on the market for new cars in Norway. When comparing this market to car markets in many other countries, two facts stand out: (i) the small size of the market, and (ii) the absence of a domestic car manufacturing industry.

In 2012, about 130,000 new cars were sold in Norway (with a population of 5.1 million), all of which were imported.¹ The five largest brands by unit sales were Volkswagen, Toyota, Volvo, Ford and Nissan, with market shares in the range of 6-13%.

Although a much larger country, South Korea (with 50 million inhabitants) is an interesting comparison, because it is at the opposite end of the spectrum in terms of the role of domestic car manufacturing. In South Korea in 2012, imported cars were less than 10% of total domestic car sales of about 1.4 million. In fact, the number of imported cars in that year was almost exactly the same as in Norway at $130,000.^2$

B. Data

For reasons of availability, the econometric analysis in this paper uses data from 2004. The data contain sales and product characteristics for all the 904 new car model variants sold in Norway in 2004.

Previous studies of the demand for cars have usually treated a model ("name plate") as one product, and have used the characteristics of the cheapest or most sold ("baseline") variant as the characteristics of the model (Berry Levinsohn and Pakes 1995). In fact, most models are marketed with a large number of different variants, varying in body type, engine size, transmission, or fuel type. Table 1 shows the 21 best-selling models (arranged by price), some characteristics of the modal variant of each of these models, along with the mean, minimum and maximum of the characteristics across variants of this model. It also shows the num-

¹ Information Council for Road Traffic, ofv.no.

 2 Korea Automobile Importers and Distributors Association, Available at: http://www.kaida.co.kr/brand/BrandMain.jsp?pageId=2&articleId=45892. The South Korean car industry produces mainly for export, however: around 60% of production is shipped abroad.

| | | | | | | | | | Paring. | 3 | | 2 | | |
|-----------------|-----------|----------|--------|--------|-------|-------|--------|-----------------|---------|--------------|-------|--------------|---------|----------------|
| | Bodytype | No. of | | Price | e | | Length | ength Cyl. vol. | Ũ | Unobs. char. | | Sales | | Rank in |
| | | variants | (mode) | (mean) | (mim) | (max) | (mode) | (mode) | (mean) | (mim) | (max) | (modal var.) | (total) | total sales |
| Volvo V70 | station | 9 | 5.26 | 5.06 | 4.32 | 5.81 | 4.71 | 2.40 | 0.70 | 0.51 | 06.0 | 887 | 2349 | 13 |
| Nissan X-Trail | SUV | 4 | 3.90 | 3.89 | 3.55 | 4.33 | 4.46 | 2.18 | 0.64 | 0.46 | 0.81 | 1647 | 2039 | 15 |
| Honda CR-V | SUV | 1 | 3.55 | 3.55 | 3.55 | 3.55 | 4.64 | 2.00 | 0.25 | 0.25 | 0.25 | 1914 | 1914 | 18 |
| Toyota RAV4 | SUV | e | 3.46 | 3.29 | 3.02 | 3.46 | 4.20 | 2.00 | 0.66 | 0.56 | 0.83 | 1305 | 2609 | п |
| Subaru Forester | station | 1 | 3.36 | 3.36 | 3.36 | 3.36 | 4.45 | 1.99 | 0.74 | 0.74 | 0.74 | 1978 | 1978 | 16 |
| VW Touran | minivan | ß | 3.17 | 3.25 | 2.95 | 3.63 | 4.39 | 1.90 | 0.35 | 0.26 | 0.52 | 2015 | 3303 | 9 |
| VW Passat | station | 13 | 3.12 | 3.47 | 2.50 | 5.58 | 4.68 | 1.90 | 0.30 | 0.18 | 0.44 | 1525 | 3501 | 5 |
| Ford Mondeo | station | 16 | 3.12 | 3.63 | 2.50 | 5.42 | 4.80 | 2.00 | 0.42 | 0.21 | 0.62 | 1710 | 3239 | 7 |
| Audi A4 | station | 24 | 3.01 | 4.55 | 2.93 | 10.34 | 4.58 | 1.60 | 0.60 | 0.27 | 0.81 | 639 | 2411 | 12 |
| Toyota Avensis | station | 17 | 3.00 | 3.29 | 2.44 | 4.30 | 4.70 | 1.79 | 0.54 | 0.35 | 0.73 | 2049 | 6301 | 1 |
| Opel Vectra | station | 17 | 2.78 | 3.28 | 2.45 | 3.72 | 4.82 | 1.80 | 0.52 | 0.40 | 0.68 | 1629 | 2996 | 8 |
| Renault Megane | minivan | 21 | 2.55 | 2.58 | 1.95 | 3.42 | 4.25 | 1.60 | 0.45 | 0.31 | 0.70 | 595 | 1884 | 20 |
| Mazda 6 | station | 12 | 2.54 | 3.11 | 2.51 | 4.00 | 4.70 | 1.80 | 0.33 | 0.25 | 0.46 | 994 | 2205 | 14 |
| Skoda Octavia | station | 11 | 2.49 | 2.59 | 1.91 | 3.27 | 4.51 | 1.90 | 0.36 | 0.07 | 0.58 | 547 | 1866 | 21 |
| Volvo S40 | station | 12 | 2.37 | 3.11 | 2.37 | 5.09 | 4.51 | 1.59 | 0.53 | 0.27 | 0.69 | 1161 | 1939 | 17 |
| Toyota Corolla | hatchback | 19 | 2.30 | 2.55 | 2.10 | 3.40 | 4.18 | 1.60 | 0.51 | 0.26 | 0.77 | 1787 | 5205 | ი |
| Ford Focus | station | 21 | 2.30 | 2.70 | 1.79 | 3.18 | 4.45 | 1.60 | 0.65 | 0.36 | 0.77 | 917 | 2712 | 10 |
| VW Golf | hatchback | 14 | 2.29 | 2.65 | 2.01 | 3.06 | 4.20 | 1.60 | 0.39 | 0.17 | 0.62 | 2697 | 5662 | 2 |
| Peugeot 307 | hatchback | 17 | 2.25 | 2.75 | 1.96 | 4.32 | 4.20 | 1.59 | 0.41 | 0.15 | 0.55 | 1272 | 4454 | 4 |
| VW Polo | hatchback | ŋ | 1.78 | 2.01 | 1.78 | 2.34 | 3.90 | 1.20 | 0.49 | 0.31 | 0.76 | 1483 | 1901 | 19 |
| Toyota Yaris | hatchback | 6 | 1.60 | 1.91 | 1.60 | 2.13 | 3.61 | 1.00 | 0.54 | 0.43 | 0.67 | 1363 | 2914 | 6 |

TABLE 1

PRODUCT CHARACTERISTICS OF BEST-SELLING PRODUCTS

SEOUL JOURNAL OF ECONOMICS

| Sales Rank in | (total) | 4 6 172 | 2 2 185 | 41 46 132 | 84 116 99 | 13 37 137 | 6 15 157 | 607 1571 25 | _ | 639 2411 12 | 649 1569 26 | 1710 3239 7 | 1525 3501 5 | 1161 1939 17 | | 2049 6301 1 | 2697 5662 2 | 731 1756 22 | 1363 2914 9 | 636 1724 23 | 82 82 111 | 63 63 120 |
|---------------|-----------------|-------------|-----------------|-------------|------------|-----------|------------------|------------------|---------------------|-------------|--------------|-------------|-------------|--------------|-----------|----------------|-------------|-------------|--------------|-------------|------------|--------------|
| ļ | x) (modal var.) | c | 4 | 8 | 4 | 6 | 4 | | | | | | | | | | | | | | 1 | 8 |
| nar. | (max) | 06.0 | 0.54 | 0.98 | 0.94 | 0.89 | 0.94 | 0.97 | 0.78 | 0.8 | 0.71 | 0.62 | 0.4 | 0.69 | 0.8 | 0.7 | 0.6 | 0.9 | 0.6 | 0.7 | 0.5 | 0.58 |
| Unobs. char. | (mim) | 0.73 | 0.54 | 0.51 | 0.07 | 0.55 | 0.60 | 0.38 | 0.20 | 0.27 | 0.08 | 0.21 | 0.18 | 0.27 | 0.16 | 0.35 | 0.17 | 0.16 | 0.43 | 0.27 | 0.51 | 0.58 |
| מ | (mean) | 0.80 | 0.54 | 0.74 | 0.40 | 0.69 | 0.79 | 0.71 | 0.50 | 09.0 | 0.45 | 0.42 | 0.30 | 0.53 | 0.47 | 0.54 | 0.39 | 0.51 | 0.54 | 0.50 | 0.51 | 0.58 |
| Cyl. vol. | (mode) | 3.60 | 5.93 | 2.93 | 2.46 | 2.97 | 3.22 | 2.15 | 2.17 | 1.60 | 1.80 | 2.00 | 1.90 | 1.59 | 1.75 | 1.79 | 1.60 | 1.60 | 1.00 | 1.12 | 1.24 | 0.80 |
| Length | (mode) | 4.43 | 4.71 | 4.95 | 4.75 | 5.05 | 5.04 | 4.82 | 4.84 | 4.58 | 4.48 | 4.80 | 4.68 | 4.51 | 4.84 | 4.70 | 4.20 | 4.25 | 3.61 | 3.83 | 3.80 | 3.49 |
| | (max) | 14.75 | 21.36 | 13.03 | 11.47 | 18.15 | 14.80 | 16.88 | 10.84 | 10.34 | 10.37 | 5.42 | 5.58 | 5.09 | 5.49 | 4.30 | 3.06 | 3.66 | 2.13 | 3.20 | 1.39 | 1.15 |
| ce | (mim) | 12.70 | 21.36 | 9.49 | 7.12 | 9.30 | 9.80 | 5.12 | 4.09 | 2.93 | 2.95 | 2.50 | 2.50 | 2.37 | 2.85 | 2.44 | 2.01 | 1.95 | 1.60 | 1.52 | 1.39 | 1.15 |
| Price | (mean) | 13.65 | 21.36 | 11.26 | 9.28 | 12.86 | 12.33 | 8.47 | 6.77 | 4.55 | 4.87 | 3.63 | 3.47 | 3.11 | 3.63 | 3.29 | 2.65 | 2.44 | 1.91 | 2.13 | 1.39 | 1.15 |
| | (mode) | 12.70 | 21.36 | 9.49 | 7.12 | 9.30 | 9.80 | 5.41 | 4.71 | 3.01 | 3.22 | 3.12 | 3.12 | 2.37 | 2.90 | 3.00 | 2.29 | 2.10 | 1.60 | 1.52 | 1.39 | 1.15 |
| No. of | variants | c, | 1 | 2 | 4 | ß | ß | 21 | 14 | 24 | 28 | 16 | 13 | 12 | 11 | 17 | 14 | 21 | 6 | 12 | 1 | 1 |
| Bodytype | modal var. v | coup | coup | SUV | SUV | sedan | sedan | sedan | sedan | station | station | station | station | station | station | station | hatch-back | hatch-back | hatch-back | hatch-back | hatch-back | hatch-back |
| | | Porsche 911 | Ast. Martin DB9 | Range Rover | VW Touareg | Audi A8 | Mercedes S-class | Mercedes E-class | BMW 5-series | Audi A4 | BMW 3-series | Ford Mondeo | VW Passat | Volvo S40 | Citron C5 | Toyota Avensis | VW Golf | Opel Astra | Toyota Yaris | Peugeot 206 | Fiat Punto | Daewoo Matiz |

TABLE 2 Product Characteristics of Sample Products

A PURE CHARACTERISTICS DEMAND MODEL 191

| Variable | Unit | Mean | Sales- weighted mean | Min | Max | Lower bound on coef- on ficient in % of price | Upper bound on coef- on ficient in % of price |
|-------------------------|--------------|------|----------------------------|----------|-------|--|--|
| length | metres | 4.44 | 4.4 | 3.49 | 5.19 | 0 | 100 |
| cylinder volume | litres | 2.1 | 1.76 | 0.8 | 6 | 0 | 100 |
| fuel costs | kroner/km | 0.68 | 0.63 | 0.27 | 1.42 | -40 | 0 |
| diesel | dummy | 0.3 | 0.28 | 0 | 1 | -20 | 60 |
| kw*diesel | kw*dummy | 0.28 | 0.24 | 0 | 2.3 | 0 | 100 |
| kw*petrol | kw*dummy | 0.78 | 0.61 | 0 | 3.68 | 0 | 100 |
| doors squared | count/10 | 1.99 | 2.26 | 0.4 | 3.6 | -60 | 60 |
| doors | count | 4.37 | 4.72 | 2 | 6 | 0 | 60 |
| seats squared | count/10 | 2.54 | 2.65 | 0.4 | 8.1 | -60 | 60 |
| seats | count | 4.97 | 5.11 | 2 | 9 | 0 | 60 |
| air bags | count | 5.29 | 5.44 | 0 | 9 | 0 | 20 |
| WD | count | 0.19 | 0.21 | 0 | 1 | -20 | 40 |
| automatic | count | 0.42 | 0.35 | 0 | 1 | -20 | 60 |
| weight | 1000 kilogr. | 1.4 | 1.32 | 0.78 | 2.52 | -60 | 60 |
| cylinders | count | 4.53 | 4.06 | 2 | 12 | -20 | 20 |
| gears*automatic | count* | 2.13 | 1.78 | 0 | 7 | 0 | 40 |
| | dummy | | | | | | |
| gears*manual | count* | 3.05 | 3.36 | 0 | 6 | 0 | 40 |
| | dummy | | | | | | |
| new model this year | dummy | 0.03 | 0.03 | 0 | 1 | 0 | 20 |
| changed model this year | dummy | 0.05 | 0.05 | 0 | 1 | 0 | 20 |
| german | dummy | 0.29 | 0.24 | 0 | 1 | -20 | 20 |
| french | dummy | 0.15 | 0.12 | 0 | 1 | -20 | 20 |
| asian | dummy | 0.21 | 0.34 | 0 | 1 | -20 | 20 |
| american | dummy | 0.15 | 0.13 | 0 | 1 | -20 | 20 |
| swedish | dummy | 0.06 | 0.08 | 0 | 1 | -20 | 20 |
| sedan | dummy | 0.24 | 0.11 | 0 | 1 | -40 | 40 |
| hatch-back | dummy | 0.23 | 0.29 | 0 | 1 | -40 | 40 |
| station wagon | dummy | 0.25 | 0.37 | 0 | 1 | -40 | 40 |
| multi-purpose/minivan | dummy | 0.11 | 0.11 | 0 | 1 | -40 | 40 |
| off-road/SUV | dummy | 0.07 | 0.11 | 0 | 1 | -40 | 40 |
| convertible | dummy | 0.06 | 0.01 | 0 | 1 | -40 | 40 |
| unobserved (estimated) | - | 0.51 | 0.52 | 0.07 | 099 | 0 | 100 |
| price | 100.000 | 4.08 | 2.96 | 1.15 | 21.36 | Coef- | |
| | kroner | | | | | -ficient | |
| | | | | | | fixed | |
| | | | | | | at -1 | |

TABLE 3SUMMARY STATISTICS

ber of variants of the model, total sales of the model, sales of the bestselling variant, as well as the model's rank in total sales. Table 2 does the same for a range of models chosen to represent the whole spectrum of car models, from the most expensive sports car through family cars to the smallest hatchback. Prices are list prices. List prices might differ from transaction prices, but these are not available apart from in smaller surveys which cover only a few products. Also, car importers in Norway usually have a policy of resale price maintenance which limits the deviations from list prices. The tables include the unobserved characteristic which is estimated in a first stage. This will be discussed in the next section.

Table 3 shows the 30 characteristics used for estimation, along with their mean across all products, the sales-weighted mean, and the minimum and maximum. It also shows the imposed bounds on the willingness to pay for one unit more of the characteristic. These bounds are discussed in subsection IV.E.

III. Literature

This section reviews parts of the literature on estimation of demand systems for differentiated products. The model in this paper can be viewed as a multidimensional extension of the vertical differentiation model of Bresnahan (1987). I therefore give an overview of that model before I summarise a recent discussion about the idiosyncratic (*e.g.* logit) taste terms in discrete-choice models.

A. Bresnahan's model of vertical differentiation

Bresnahan (1987) estimates car demand using a vertical differentiation model like those in Mussa and Rosen (1978) and Shaked and Sutton (1982). In this model a consumer's utility is

$$u_{ij} = x_j \beta_i - p_j, \tag{1}$$

where the characteristic, x_{j} , is a scalar representing "quality."³ The taste parameter β has an estimated density on a nonnegative support, so that all consumers have a positive marginal valuation of the characteristic. Consumers make different choices because they have different valuations of the characteristic relative to price.

Utility for each product can be pictured as a linear function of β , where $-p_j$ is the intercept with the vertical axis, and x_j is the gradient. Each consumer is located somewhere on the horizontal axis, and chooses the product with the utility line that is highest at this β -value. For all

 $^{^3}$ Quality is an estimated function of characteristics. The important thing in this context is that quality is the same for all consumers.

194 SEOUL JOURNAL OF ECONOMICS

products to have positive demand, it must be the case that if one product has strictly lower quality than another, it also has a strictly lower price. It follows that the utility lines are ordered in a pattern where the lowestquality product has the highest-lying line close to the vertical axis, because it has the highest vertical intercept (lowest price). At some point, this line is crossed by the product which is above it in the quality ranking (steeper slope). For high enough β s, this line is superseded by the third-lowest quality product, and so on. In general, the point where the utility lines for products *j* and *j*+1 cross is given by

$$\beta^{j,j+1} = \frac{p_{j+1} - p_j}{x_{j+1} - x_j}.$$
(2)

If products are indexed in order of increasing quality, product js market share is

$$F_{\beta}(\beta^{j,j+1}) - F_{\beta}(\beta^{j-1,j}),$$
(3)

where F_{β} is the cumulative distribution function of β , or the distribution of willingness to pay for quality in the population of consumers.

Bresnahan assumes a uniform density for β . Demand for a product is then proportional to the length of the interval on the horizontal axis where this product's utility line is the highest:

$$q_{j} = \delta \cdot [\beta^{j,j+1} - \beta^{j-1,j}] = \delta \cdot [\frac{p_{j+1} - p_{j}}{x_{j+1} - x_{j}} - \frac{p_{j} - p_{j-1}}{x_{j} - x_{j-1}}],$$
(4)

where δ is the (constant) density function. The cross-price and own-price demand derivatives are $(\delta/(x_{j+1}-x_j))$ and $-(\delta/(x_{j+1}-x_j))-(\delta/(x_j-x_{j-1}))$, so the more similar the products are in terms of quality, the higher the price elasticities. Graphically, price substitution happens in the following way: When the price of a product goes up, its utility line shifts down, since the vertical intercept, -p, is lower. This means that the point where it rises above the utility of the lower-quality neighbour is shifted outwards, and the point where it is superseded by its higher-quality neighbour is shifted inwards, shrinking the interval where it is above the other lines.

B. Idiosyncratic tastes

Caplin and Nalebuff (1991) point out that including idiosyncratic error terms (as in a logit model) in utility is equivalent to including a dummy for every product, and imposing draws from the chosen distribution⁴ as the coefficients on these dummy variables. This implies that the introduction of a new product adds one dimension to unobserved characteristics space. Since the expected difference between the logit term of any two products is the same regardless of the number of products, there is no congestion in unobserved characteristics space (Ackerberg and Rysman 2005). This is counterintuitive in the sense that one would expect products to become closer as their number increases, as in a Hotelling model. Congestion does occur in the observed part of characteristics space, but the additional dimension of unobserved characteristics space allows every new product to be differentiated in a new way. The lack of congestion appears to overestimate the benefit of variety to consumers (Petrin 2002). One would expect that as the number of products goes to infinity, every product should have a perfect substitute, *i.e.* that every consumer could substitute to some other product with zero utility loss. Bajari and Benkard (2003) show that in any logit model such utility losses are bounded away from zero in the limit.

Ackerberg and Rysman (2005) propose to let the distribution of the idiosyncratic term change with the number of products in the choice set, to allow for congestion of product space. Berry and Pakes (2007) do away with the idiosyncratic term altogether, giving rise to a pure characteristics model. In this paper I estimate a model based on the pure characteristics model of Bajari and Benkard (2005). That model will be discussed in detail in the next section. Blow, Browning, and Crawford (2008) estimate a nonparametric characteristics-based demand model for milk.

IV. Model and Identification

A. The model

There are *J* products defined as bundles of *K* characteristics (x_j, ξ_j) , where $x_j \in \mathbb{R}^{K-1}$ is observed, and $\xi_j \in \mathbb{R}$ is not observed by the researcher. The unobserved characteristic represents such things as style, quality and service, collapsed into a scalar value. Each consumer chooses one

⁴ Type 1 extreme value in the case of the logit model.

196 SEOUL JOURNAL OF ECONOMICS

product. This is the product which maximises his or her utility over the set of all products. Utility is a linear function of the product characteristics and price. The fact that consumers choose different products is only due to differences in their willingness to pay for characteristics. The final goal of the analysis is to estimate the joint distribution of the taste coefficients, *i.e.* the linear coefficients in the utility function.

A consumer's ranking of alternatives is unaffected by the scale of utility. Utility can therefore be multiplied by an individual-specific constant without changing the consumer's utility-maximising choice. The following normalisation is therefore permitted: all price coefficients are set to -1 (multiply by individual-specific constant, the inverse of the price coefficient).⁵ Utility is then given by

$$u_{ij} = x_j \beta_i - p_j, \tag{5}$$

where *i* indexes individuals and *j* indexes products. For simplicity of notation, the vector x_j includes the unobserved characteristic as well as all the other characteristics.

B. The hedonic price function

Using the assumption that utility is strictly increasing in the unobserved characteristic ξ for all products and for all consumers (and two mild regularity conditions), Bajari and Benkard (2005) show that for any two products *j* and *f* with strictly positive demand, it must be true that

1. If $x_j = x_j$ and $\xi_j = \xi_j$, then $p_j = p_j$. 2. If $x_j = x_j$ and $\xi_j > \xi_j$, then $p_j > p_j$. 3. $|p_j - p_f| \le M(|x_j - x_f| + |\xi_j - \xi_f|)$ for some $M \le \infty$.

Using these properties, we can define a mapping from observed and unobserved characteristics to price. Because of 1 the mapping is a function, since a point in the domain of the mapping maps to a unique point in its image set. Because of 2 the mapping is strictly increasing in the unobserved characteristic. Because of 3 the mapping defines a (Lipschitz) continuous surface. The price surface is denoted $p(x, \xi)$. In a

 $^{^5\,\}mathrm{In}$ logit and probit models this normalization is achieved by fixing the variance of the error term.

logit demand model, such a surface does not necessarily exist, since two products with the same characteristics and different price can both have strictly positive demand, because of the idiosyncratic taste term. The price function depends on the nature of competition, marginal costs, consumer preferences, and the products present in the market. If any of these primitives change, the shape of the price surface is also likely to change. The price function expresses the relationship between prices and characteristics in equilibrium in a particular market. See Bajari and Benkard (2005) pp. 1247-8 for a discussion of the price function.

C. Identification of the unobserved characteristic

The assumption used for identification is that the unobserved characteristic is independent of the observed characteristics.⁶ The unobserved characteristic has no inherent units, and so it is only identified up to a monotonic transformation. It is therefore normalised so the marginal distribution of ξ is U(0, 1). Bajari and Benkard (2005) use an identification result from (Matzkin 2003): $\{\xi_j\}_{j=1,...,J}$ is identified when the prices of many products are observed in a market, so that the joint distribution F(p, x) is known. The proof is:

$$F_{p|x=x_{j}}(p_{j}) = Pr(p(x,\xi) \le p_{j} | x = x_{j})$$

= $Pr(\xi \le p^{-1}(x, p_{j}) | x = x_{j})$
= $Pr(\xi \le p^{-1}(x_{j}, p_{j}))$
= $p^{-1}(x_{j}, p_{j})$
= ξ_{j} (6)

The second line holds since the price function has an inverse for a given *x* since it is strictly increasing and continuous in ξ . The third line holds by the independence between *x* and ξ . The fourth line holds because the *q*-quantile of U(0, 1) equals *q*.

D. Identification of the taste coefficients

In the second stage, the unobserved characteristic recovered in the first stage is given, and treated in the same way as the observed char-

 $^{^6\,\}rm This$ assumption is slightly stronger than the mean independence assumption in Berry, Levinsohn, and Pakes (1995). Manski (1994) discusses alternative moment conditions.

198 SEOUL JOURNAL OF ECONOMICS

acteristics. For notational convenience, it is therefore included as one of the elements of the *x*-vector. For product j to maximise utility, it must be the case that

$$x_{j}\beta - p_{j} \ge x_{l}\beta - p_{l}, \quad \forall l \neq j.$$
⁽⁷⁾

Let \tilde{X}_j be the $(J-1) \times K$ -matrix whose rows are the $(1 \times K)$ -vectors $x_j - x_h$, l=1, ..., j-1, j+1, ..., J, and let \tilde{p}_j be the j-1 vector with elements $p_j - p_h$ running over the same indices as \tilde{X}_j . Then the condition that product j maximises utility can be written as a system of linear inequalities on standard matrix form. The set of taste coefficients permitted by the revealed preference condition (7) for product j is

$$A_{i} \equiv \{\beta \mid \tilde{X}_{i}\beta \leq \tilde{p}_{i}\}.$$
(8)

This means that if a consumer chooses product *j*, his or her vector of taste coefficients must be inside the *K*-dimensional convex polyhedron A_j . The market share of a product is the share of the population with taste vectors falling within the polyhedron corresponding to that product.

E. Bounds on willingness to pay

For a given characteristic, such as horsepower, the revealed preference inequalities in (7) imply no upper bound on the coefficient for those consumers who buy the product with the highest value of that characteristic. In the same way, there is no lower bound for the consumers buying the product with the lowest value of a characteristic.

This problem is limited in the case of continuous characteristics, since there will usually be only one product attaining the maximum (and one attaining the minimum) for each characteristic. For indicator variables ('has a diesel engine'), however, all products are either the maximum or minimum of that characteristic. This means that none of the *A*-sets (sets of coefficients that rationalise a given choice) will be bounded. Leaving the coefficient for some characteristics unbounded also has repercussions in the sense that an extremely high value for one characteristic often must be matched by an extreme value of another characteristic in order for the product to be the utility maximiser.

To deal with this problem I impose conservative bounds on the coefficients. Since the price coefficient is normalised to -1, the coef-

ficients of the characteristics have the convenient interpretation of willingness-to-pay for a one unit increase in the value of that characteristic. Accordingly, the bounds are formulated as bounds on the willingness to pay for characteristics, given as a percentage of the price of the product in question. (The bounds are shown in Table 3.) For example, a consumer's willingness to pay for an additional litre of cylinder volume is bounded above by 100% of the price of the car that the consumer actually bought. So if a consumer buys a car that costs 300.000 kroner (appr. \$ 50,000), it is assumed that his willingness to pay for an additional 1 litre of cylinder volume on a car is bounded above by 300.000 kroner. For some characteristics it is assumed that willingness-to-pay is bounded below by zero, *i.e.* that nobody would pay a positive amount of money to have less of these characteristics. On the other hand, this possibility is allowed for many characteristics. For instance, if somebody does not like German cars, he or she may be willing to pay a little extra to have a car which is not German. The constraints are meant to be conservative, and it appears unlikely that they should be violated by the true distribution of taste coefficients.

F. Distribution of tastes within the bounds

While the revealed-preference inequalities provide bounds (the A polyhedra) on the taste coefficients of the consumers who choose each product, they tell us nothing about the distribution of tastes within these bounds. When the number of products goes to infinity in such a way that the A-sets are partitioned ever more finely, in the limit these sets will be points (see Bajari and Benkard (2005) for a proof). Accordingly it can be expected that with a large number of products, the distribution of probability mass inside these sets will not be important. I impose the assumption that the distribution of consumer tastes within each set A_j is uniform. (See section V.B for further details.)

V. Estimation

A. First stage

The unobserved characteristic is given in (6) as a quantile of a conditional distribution: $F_{p|x=x_j}(p_j)$. The nonparametric estimation of conditional distribution functions and quantiles are well known problems. Matzkin (2003) suggests the following estimator, based on Nadaraya (1964):

$$\hat{F}_{p|x=x_j}(p_j) = \frac{\sum_{i=1}^{J} \tilde{k}_i(\frac{p_j - p_i}{h}) k_2(\frac{x_j - x_i}{h})}{\sum_{i=1}^{J} k_2(\frac{x_j - x_i}{h})},$$
(9)

where $k_2(\cdot)$ is a multidimensional kernel, $\tilde{k}_1(u) = \int_{-\infty}^u k_1(s) ds$, and *h* is the bandwidth.

My data have around 900 products and 30 characteristics. It is difficult to estimate a quantile of a 30-dimensional density using just 900 data points. I follow (Bajari and Benkard 2005) in assuming that the price function is additively separable in most of the characteristics, and then estimate the nonadditive part nonparametrically after removing the linear effects of the other variables. The price function is then $p(x, \xi) = p(x^A, \xi)$ $+x^B \hat{\gamma}$, where (x^A, x^B) is a partitioning of the vector x.⁷ The $\hat{\gamma}$ is the OLS estimate from the regression

$$p_j = x_j^A \theta + x_j^B \gamma + e_j.$$
⁽¹⁰⁾

The price data used for the nonparametric estimation of the unobserved characteristic are

$$\tilde{p}_j = p_j - x_j^B \hat{\gamma}. \tag{11}$$

I used Epanechnikov kernels for the estimator in (9) (see for instance Martinez and Matinez (2002)):

$$k_1(\psi) = \frac{3}{4} (1 - \psi^2), \quad -1 \le \psi \le 1$$
(12)

The bandwidths were chosen according to the Epanechnikov bandwidth rule (see Azzalini (1981)) $h=1.3\hat{\sigma}n^{-1/3}$, where *n* is the number of observations and $\hat{\sigma}$ is the empirical standard deviation of the data.

B. Second stage

I use a multi-stage Gibbs sampler to take random draws from the *A*-sets. The Gibbs algorithm is a general principle that can be used to draw

$$^{7} x^{A}$$
 = (horsepower, cyl.vol., length).

200

A PURE CHARACTERISTICS DEMAND MODEL

from a multivariate density f(x) which is difficult to draw from directly, but whose univariate conditional densities can be drawn from. Take a starting value $x^{(l)}$, and generate $X_1^{(l+1)}$: $f_1(x_1 | x_2^{(l)}, x_K^{(l)})$, then $X_2^{(l+1)}$: $f_2(x_2 | x_1^{(l+1)}, x_3^{(l)}, x_K^{(l)})$, and so on. As the number of iterations gets large, the distribution of *x* approaches f(x) (Robert and Casella 2004).

The revealed preference condition for the coefficient of characteristic 1 as given in (7) can be rewritten as, for all $l \neq j$,

$$\beta_{1} \geq \frac{\sum_{k \neq 1} \beta_{k} (x_{l,k} - x_{j,k}) - (p_{l} - p_{j})}{x_{j,1} - x_{l,1}} \quad \text{if} \quad x_{j,1} > x_{l,1}$$
(13)

$$\beta_{1} \leq \frac{\sum_{k \neq 1} \beta_{k} (x_{l,k} - x_{j,k}) - (p_{l} - p_{j})}{x_{j,1} - x_{l,1}} \quad \text{if } x_{j,1} < x_{l,1}, \tag{14}$$

and similarly for the other coefficients. Denote the right hand side of the inequalities above B(j, l, 1). This means that in general, for the product j, every other product provides either an upper or a lower bound on the coefficient values which could lead to the purchase of product j. The bounds based on willingness-to-pay, as described above, denoted as \underline{b}_1 and \overline{b}_1 , provide additional constraints.

The distribution of probability mass inside each *A*-set is uniform, as discussed in the previous section.⁸ Given a starting value, $\beta_j^{(0)}$, which is inside A_p it must be true that

$$\beta_{j,1} \mid \beta_{j,2}^{(0)}, \dots, \beta_{j,K}^{(0)} \square \mathcal{U}(\beta_{j,1,\min}, \beta_{j,1,\max}),$$
(15)

where the parameters of the univariate uniform depends on the conditioned-on betas in the following way:

$$\beta_{j,1,\min} = \max\{\underline{b}_{j,1}, \max\{B(j,l,1) \mid l \neq j \text{ and } x_{j,1} > x_{l,1}\}\}$$
 (16)

$$\beta_{j,1,\max} = \min\{b_{j,1}, \min\{B(j,l,1) \mid l \neq j \text{ and } x_{j,1} < x_{l,1}\}\}.$$
 (17)

⁸ Even if this assumption were not maintained, random draws under the assumption of a uniform distribution will reveal the support of the random vector β_{ρ} and this support is precisely the set A_{ρ}

Given the starting value, $\beta_j^{(0)}$, the algorithm follows the Gibbs procedure described above, with equations (15-17) describing the conditional densities that are drawn from at each stage.

The Gibbs sampler is computationally straightforward. The most challenging part was to find a starting point, *i.e.* any point satisfying (7). Bajari and Benkard (2005) report that they used as starting values coefficients derived from first-order conditions under the assumption that product space is filled up (so that consumers can pick a product anywhere in characteristics space). This method did not work for my data. The only method which turned out to be reliable was to use the centre of the Chebyshev ball (the largest *K*-dimensional ball wich can be fit inside the polyehedron), computed by Komei Fukuda's *cdd*⁹ code, implemented for Matlab in *MPT* (Herceg, Kvasnica, Jones, and Morari 2013).

To draw from the full joint distribution of the betas, I use $ns_j=1500$ draws for each product *j*. An initial 1500 draws are burn-in draws for the Gibbs sampler. Each draw from A_j is weighted by the market share of product *j*. The simulated market share, used to compute price elasticities, is

$$\breve{s}_{j} = \sum_{l=1}^{J} s_{l} \frac{1}{ns_{l}} \sum_{i=1}^{ns_{l}} \mathbb{1}(c_{li} = j),$$
(18)

where s_i is the observed market share of product *l*, *i.e.* the proportion of car buyers whose coefficients are in the set A_i , c_{ii} denotes the product which maximises utility given the *i*-th draw of coefficient vector from A_i , $\mathbf{l}(\cdot)$ is the indicator function.

To clarify, when prices and product characteristics are at their observed values, all ns_j draws for product j result in the choice of j, so that $\frac{1}{ns_j} \sum_{i=1}^{ns_j} 1(c_{ji} = j) = 1$. Substitution effects show up when prices change, and some of the draws for product j result in the purchase of a different product, so that $\frac{1}{ns_j} \sum_{i=1}^{ns_j} 1(c_{ji} = j) < 1$. At the same time, draws from a different product could now result in the purchase of product j. (The draws for product j represent the taste distribution of consumers who actually purchased product j.)

⁹ Komei Fukuda (Available at: http://www.inf.ethz.ch/personal/fukudak/cdd home/index. html).

202

VI. Results

A. The unobserved characteristic

The estimated unobserved characteristic ranges from 0.07 to 0.99 and has a mean of 0.52. Tables 1 and 2 show the value of the unobservable for the modal variant of a selection of models, as well as its mean, minimum and maximum across variants of each model. The unobserved characteristic is independent of all other characteristics (not including price). Generally speaking, a product with a high price relative to its characteristics will have a high value of the unobserved characteristic, since high quality, style or prestige is required for it to have positive demand in the presence of other, cheaper products with similar observed characteristics. This is illustrated by table 4. All Mercedes E-class variants have high values of the unobserved characteristic. This is consistent with the perception of Mercedes as a prestigious brand. The Peugeot 607 is a comparable car to the Mercedes E for similar engine sizes. A comparison reveals that the unobserved characteristic is lower for the Peugeot for similar specifications, presumably reflecting the higher prestige of the Mercedes. A similar pattern is found by comparing the Audi A4 with the Skoda Octavia, two similar models where the first is regarded as more prestigious than the second.

The low-end Mercedes E variants have extremely high values for the unobserved characteristic, reflecting some feature which gives them positive demand in spite of their very high prices relative to observed characteristics. Each variant is a package of characteristics, and the prestige derived from a big engine or a German manufacturer goes into those observed characteristics. The unobserved characteristic can therefore not simply be interpreted as prestige or quality, but rather as the amount of prestige or quality that the car has beyond what is derived from its observed characteristics. Accordingly, a 5 litre top-of-the-range Mercedes E is indeed more prestigious than the bottom-of-the-range 1.8 litre version, but it is already clear from its observed characteristics that it is a high-prestige product. This is not the case with the 1.8 litre version, however, and the model therefore assigns it a higher unobserved characteristic. Compared to a 2 litre Peugeot 607 which sells for 365,000 kroner, the 1.8 litre Mercedes must have substantial unobserved merit in order to warrant its 512,000 kroner price tag.

| UNOBSERVED | CHARAC | TERISTICS | FOR SAM | MPLE MO | DELS WITH | VARIANTS |
|----------------|--------|-----------|---------|---------|-----------|--------------|
| Make | Model | Cyl.vol. | Length | Price | Bodytype | Unobs. char. |
| 'Mercedes-Benz | Е | 1.8 | 4.8 | 5.12 | sedan | 0.90 |
| 'Mercedes-Benz | E | 1.8 | 4.8 | 5.60 | station | 0.96 |
| 'Mercedes-Benz | E | 2.2 | 4.8 | 5.41 | sedan | 0.95 |
| 'Mercedes-Benz | E | 2.2 | 4.8 | 5.94 | station | 0.97 |
| 'Mercedes-Benz | E | 2.6 | 4.8 | 6.03 | sedan | 0.69 |
| 'Mercedes-Benz | Е | 2.6 | 4.8 | 6.40 | sedan | 0.78 |
| 'Mercedes-Benz | Е | 2.6 | 4.8 | 6.30 | sedan | 0.79 |
| 'Mercedes-Benz | E | 2.6 | 4.8 | 6.50 | station | 0.77 |
| 'Mercedes-Benz | Е | 2.6 | 4.8 | 6.90 | station | 0.85 |
| 'Mercedes-Benz | E | 2.6 | 4.8 | 6.81 | station | 0.85 |
| 'Mercedes-Benz | E | 3.2 | 4.8 | 7.52 | sedan | 0.62 |
| 'Mercedes-Benz | Е | 3.2 | 4.8 | 7.87 | sedan | 0.72 |
| 'Mercedes-Benz | Е | 3.2 | 4.8 | 7.35 | sedan | 0.65 |
| 'Mercedes-Benz | E | 3.2 | 4.8 | 8.35 | station | 0.78 |
| 'Mercedes-Benz | Е | 3.2 | 4.8 | 7.84 | station | 0.74 |
| 'Mercedes-Benz | Е | 4.0 | 4.8 | 10.07 | sedan | 0.38 |
| 'Mercedes-Benz | E | 5.0 | 4.8 | 11.17 | sedan | 0.39 |
| 'Mercedes-Benz | E | 5.0 | 4.8 | 11.50 | sedan | 0.44 |
| 'Mercedes-Benz | E | 5.0 | 4.8 | 11.93 | station | 0.47 |
| 'Mercedes-Benz | Е | 5.4 | 4.8 | 16.30 | sedan | 0.60 |
| 'Mercedes-Benz | E | 5.4 | 4.8 | 16.88 | station | 0.63 |
| 'Peugeot | 607 | 2.0 | 4.8 | 3.65 | sedan | 0.59 |
| 'Peugeot | 607 | 2.0 | 4.8 | 3.85 | sedan | 0.76 |
| 'Peugeot | 607 | 2.2 | 4.8 | 4.25 | sedan | 0.66 |
| 'Peugeot | 607 | 2.2 | 4.8 | 4.45 | sedan | 0.81 |
| 'Peugeot | 607 | 3.0 | 4.8 | 5.85 | sedan | 0.22 |
| 'Audi | A4 | 1.6 | 4.6 | 2.93 | sedan | 0.62 |
| 'Audi | A4 | 1.6 | 4.6 | 3.01 | station | 0.65 |
| 'Audi | A4 | 1.8 | 4.6 | 3.80 | sedan | 0.51 |
| 'Audi | A4 | 1.8 | 4.6 | 4.00 | sedan | 0.53 |
| 'Audi | A4 | 1.8 | 4.6 | 3.33 | sedan | 0.43 |
| 'Audi | A4 | 1.8 | 4.6 | 3.81 | sedan | 0.66 |
| 'Audi | A4 | 1.8 | 4.6 | 3.98 | station | 0.62 |
| 'Audi | A4 | 1.8 | 4.6 | 4.19 | station | 0.63 |
| 'Audi | A4 | 1.8 | 4.6 | 3.52 | station | 0.53 |
| 'Audi | A4 | 1.8 | 4.6 | 4.00 | station | 0.75 |
| 'Audi | A4 | 2 | 4.6 | 3.39 | sedan | 0.63 |
| 'Audi | A4 | 2 | 4.6 | 4.76 | sedan | 0.59 |
| 'Audi | A4 | 2 | 4.6 | 3.81 | sedan | 0.73 |
| 'Audi | A4 | 2 | 4.6 | 3.54 | station | 0.70 |
| 'Audi | A4 | 2 | 4.6 | 4.76 | station | 0.66 |
| 'Audi | A4 | 2 | 4.6 | 4.01 | station | 0.81 |

 TABLE 4

 UNOBSERVED CHARACTERISTICS FOR SAMPLE MODELS WITH VARIANTS

(Table 4 Continued)

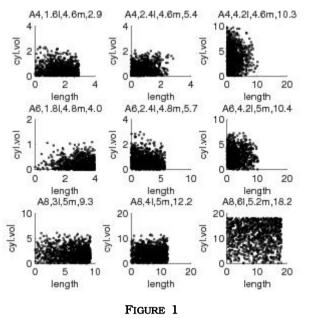
| | | | ONTINOED | | | |
|--------|---------|----------|----------|-------|-----------|--------------|
| Make | Model | Cyl.vol. | Length | Price | Bodytype | Unobs. char. |
| 'Skoda | OCTAVIA | 1.4 | 4.6 | 1.91 | station | 0.47 |
| 'Skoda | OCTAVIA | 1.6 | 4.6 | 2.25 | hatchback | 0.29 |
| 'Skoda | OCTAVIA | 1.6 | 4.6 | 2.28 | station | 0.43 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.71 | hatchback | 0.45 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 3.20 | station | 0.07 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 3.27 | station | 0.34 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.49 | station | 0.40 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.90 | station | 0.58 |
| 'Skoda | OCTAVIA | 2.0 | 4.6 | 2.49 | hatchback | 0.28 |
| 'Skoda | OCTAVIA | 2.0 | 4.6 | 3.07 | hatchback | 0.24 |
| 'Skoda | OCTAVIA | 1.4 | 4.6 | 1.91 | hatchback | 0.43 |
| 'Skoda | OCTAVIA | 1.4 | 4.6 | 1.91 | station | 0.47 |
| 'Skoda | OCTAVIA | 1.6 | 4.6 | 2.25 | hatchback | 0.29 |
| 'Skoda | OCTAVIA | 1.6 | 4.6 | 2.28 | station | 0.43 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.71 | hatchback | 0.45 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 3.20 | station | 0.07 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 3.27 | station | 0.34 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.49 | station | 0.40 |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.90 | station | 0.58 |
| 'Skoda | OCTAVIA | 2.0 | 4.6 | 2.49 | hatchback | 0.28 |
| 'Skoda | OCTAVIA | 2.0 | 4.6 | 3.07 | hatchback | 0.24 |

TABLE 4

B. Taste coefficients

The draws generated in the second stage of the estimation are uniformly distributed inside the 30-dimensional revealed-preference polyhedra. Figure 1 shows scatter plots of the joint densities of the taste coefficients for length and cylinder volume of consumers who buy three different variants of each of the models Audi A4, A6 and A8. The variants are the bottom-of-the-range, a middle-of-the-range, and the top-of-therange variants of each model in terms of price and engine size. The scatter plots are the projections of points distributed in a 30-dimensional space onto a 2-dimensional space. This explains why the sets do not look like polyhedra and the points do not look like they are uniformly distributed.

Taste coefficients for length and cylinder volume are bounded below by zero and above by the price of the product the consumer has chosen (cf. table 3). In the discussion of the bounds I said that they are meant to be conservative bounds, and that they are unlikely to be violated by



SCATTER PLOTS OF JOINT DENSITIES OF TASTE COEFFICIENTS FOR SAMPLE PRODUCTS

the true taste distribution in the population. At the same time, the model is not identified without these bounds. This means that the distribution of taste coefficient draws generated by the model *will* be constrained by the bounds to varying degrees.

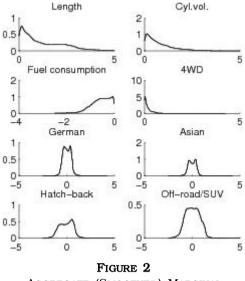
It is clear that in the case of the top A8, the bounds severely restricts the area within which the draws fall, as points accumulate close to the upper bounds. Since the biggest A8 faces few or no competitors that are longer or have a bigger engine, revealed preference does not constrain the draws upwards. The mid A4, on the other hand, is located in a very densely occupied area of characteristics space. The large number of close competitors means that revealed preference provides upper constraints that are well below the upper bounds on willingness-to-pay.

Comparing the top or mid A4 with the bottom and mid A6 reveals an interesting pattern. The A4 is smaller than the A6, but otherwise the two models are similar with respect to design, quality and service. The different choices of buyers of the A4 and buyers of the A6, should therefore be due to a large extent to different tastes for length. This is indeed confirmed. Mid A4 buyers have a similar distribution of taste for

volume to mid A6 buyers (cylinder volume being the same), but markedly lower tastes for length. The reason to pay 30.000 kroner to get an A6 instead of a very similar, but slightly shorter A4, is that the willingnessto-pay for length is high. Some consumers who buy the top A4 have high willingness-to-pay for cylinder volume, but not for length. Conversely, bottom A6 buyers care little about engine size, but have a very strong taste for length. The same pattern is confirmed by comparing the A6 and the A8.

To find the aggregate distribution of taste parameters, the draws for each of the 904 variants are aggregated, and weighted by the market share of each car, corresponding to the proportion of consumers represented by those particular draws. Since probability mass is assumed to be uniformly distributed inside each taste coefficient polyhedron, the approximation to the true aggregate taste distribution will be better if each polyhedron is small in some sense. As discussed in the identification section, if the number of products goes to infinity in such a way that all polyhedra collapse to points, the distribution resulting from the model will equal the true distribution in the limit. The scatter plots in Figure 1 give the impression that the polyhedra are relatively large. However, if one imagines a 30-dimensional rectangle with sides similar to those formed by the scatter plot of the top A8, this 30-dimensional rectangle will contain all 904 taste coefficient polyhedra. These polyhedra are disjoint, and so much smaller than the rectangle which contains them all. Furthermore, most polyhedra are contained in a much smaller volume, with a few fringe products like the top Audi A8 having much larger polyhedra.

Figure 2 shows kernel smoothed graphs of the aggregate marginal densities of some taste coefficients. Compared to the scatter plots in Figure 1, where points look almost uniformly distributed, these densities have much more probability mass concentrated at certain (low) levels. The products with high sales are concentrated in certain areas of characteristics space. In practice that means that many people have tastes leading them to prefer products in those areas. For the purposes of this discussion, that in turn means that draws in those areas are given much larger (market share) weights. All the marginal densities have peaks relatively close to zero. This is most marked in the cases of length and cylinder volume. These coefficients are well constrained by revealed preference, because the corresponding characteristics are continuous and exhibit large variation in the data. The marginal densities for some dummy variables have less sharp peaks, because their taste coefficients



Aggregate (Smoothed) Marginal Densities of Some Taste Coefficients

are not identified as well by the revealed preference bounds.

Berry, Levinsohn, and Pakes (1995) assume independence between the taste coefficients for different characteristics. Figure 3 shows kernel smoothed pairwise joint aggregate densities for some taste coefficients. The graphs exhibit some interesting examples of dependence between taste parameters that would be ruled out by assuming independence. First, there is a substantial proportion of the population with a relatively high taste for both cylinder volume and length, whereas very few people have high tastes for only one of these characteristics and not the other. Secondly, there are many consumers with strong preferences for both four-wheel drive and a SUV body type. This is not surprising, but certainly not a feature that should be ruled out by distributional assumptions. Thirdly, an inverse relationship exists between taste for cylinder volume and disutility of fuel costs. Again a substantial group of consumers have a very low disutility of fuel costs and at the same time a very high preference for cylinder volume, whereas hardly anyone has such high tastes for cylinder volume while at the same time disliking fuel costs very much. Finally, the perhaps most interesting example shows that there is a strong inverse relationship between tastes for German cars and tastes for Japanese or Korean cars. Especially, consumers

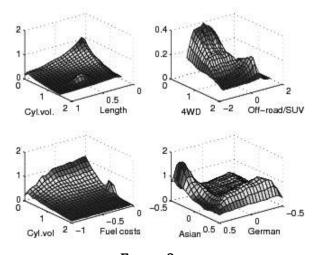


Figure 3 Aggregate (Smoothed) Pairwise Joint Densities of Some Taste Coefficients

who have a high willingness to pay for their car being German, get a high disutility from an Asian car. Also, many consumers who value Asian cars dislike German cars. These examples seem intuitive, and appear to support the case that independence between taste parameters is an undesirable assumption.

C. Substitution patterns

Elasticities were computed by finding the numerical derivative of the simulated market shares given by (18) w.r.t. each product. I did this in two ways. Under method I consumers face a choice set containing all variants of every model, leaving them with 904 choices. Derivatives were computed with finite differences by letting the price increase for all variants of the relevant model, and then looking at how the joint market share of all variants of the model changed.¹⁰ To turn the derivatives into elasticities, they where multiplied by the price of the modal (best-selling) variant, and divided by the original joint market share.

In method II, I removed all variants apart from the modal variant of

 $^{^{10}\,\}rm I$ increase the prices of all variants of a model rather than one at a time because I am particularly interested in substitution between models, since this has been the focus of the literature.

each model from the choice set, and simulated demands with this new choice set. I then computed derivatives in the same way as for model I.

The median own price elasticity from method I was -35, and -13 in method II. Berry, Levinsohn, and Pakes (1995) report own price elasticities that mostly range from -3 to -6. Table 5 shows the own price elasticities, markups (price minus marginal cost) and markups as a percentage of price for the 50 best selling products in the market, computed using method II and the assumption of a Nash equilibrium in prices, with profit maximising entities being the 16 car manufacturing companies which produce the 197 products on the market. The executive/big family type cars at the top of Table 5 (Mercedes E to Saab 9.5) all have relatively high markups, ranging from 19 to 32%. This is consistent with the observation that these models are in a niche with few competitors of similar regard. Further down the list markups are generally lower, consistent with the fact that characteristics space is more crowded in that area.

In Tables 6-9 each row shows the elasticities for a car with respect to the price of the cars in each column. Tables 6 and 7 are elasticities computed with method I, and Tables 8 and 9 are elasticities computed with method II. In Tables 6 and 8, the models displayed are the ones used previously to represent the spectrum of choices in the market, while Tables 7 and 9 display the top selling 21 cars. Products have been arranged with the most expensive in the top-left corner, and the cheapest in the bottom-right corner.

The elasticities for the representative sample of cars in Table 6 exhibit a pattern where cross-price elasticities of cars that are far away from each other are zero or very low. Accordingly the areas furthest away from the diagonal mostly mostly consist of zeros. On the diagonal are ownprice elasticities, and broadly speaking, as one moves further away from the diagonal, one gets to cross elasticities with products that are more different. In the top left and the bottom right areas of the matrix, the belt of positive cross elasticities around the diagonal is thin. Since these extreme areas represent products at the fringes of characteristics space, they have fewer substitutes. Moving towards the middle of the matrix, where characteristics space is more densely filled with products, the belt around the diagonal gets thicker, since products have more substitutes. Moving away from the diagonal, it is generally true that cross elasticities gradually get lower, as they represent products that are gradually more different from the product at the diagonal. Cross elasticities higher than one are normally only found for adjacent or almost adjacent

| Make | Model | Cyl. vol. | Price | Markup (P-MC) | Markup as % of price | Own price elast- icity | Units sold modal var. | Units sold total | Sales modal % of total |
|---------------------|-----------------|--------------|--------------|------------------|-------------------------------|---------------------------------|--------------------------------|------------------------|---------------------------------|
| 'Mercedes-Benz | E | 2.2 | 5.4 | 1.1 | 21 | -5.4 | 607 | 1571 | 39 |
| 'Volvo | V70 | 2.4 | 5.3 | 1.1 | 21 | -5.8 | 887 | 2349 | 38 |
| 'Bmw | 5 | 2.2 | 4.7 | 1.5 | 32 | -3.2 | 545 | 1049 | 52 |
| 'Audi | A6 | 1.8 | 4.4 | 0.8 | 19 | -7.5 | 470 | 1614 | 29 |
| 'Saab | 9.5 | 2.0 | 4.1 | 1.1 | 26 | -3.8 | 812 | 1406 | 58 |
| 'Nissan | X-TRAIL | 2.2 | 3.9 | 0.5 | 12 | -9.0 | 1647 | 2039 | 81 |
| 'Mercedes-Benz | С | 1.8 | 3.7 | 0.3 | 7 | -14.9 | 515 | 1160 | 44 |
| 'Honda | CR-V | 2.0 | 3.5 | 1.3 | 36 | -3.0 | 1914 | 1914 | 100 |
| 'Subaru | LEGACY | 2.0 | 3.5 | 0.3 | 9 | -19.5 | 639 | 1050 | 61 |
| "Toyota | RAV4 | 2.0 | 3.5 | 0.4 | 12 | -8.5 | 1305 | 2609 | 50 |
| 'Mitsubishi | OUTLANDER | 2.0 | 3.4 | 0.5 | 15 | -7.1 | 721 | 1106 | 65 |
| 'Subaru | FORESTER | 2.0 | 3.4 | 0.3 | 10 | -10.6 | 1978 | 1978 | 100 |
| 'Bmw | 3 | 1.8 | 3.2 | 0.2 | 7 | -13.5 | 649 | 1569 | 41 |
| Volkswagen | TOURAN | 1.8 | 3.2 | 1.0 | 32 | -3.9 | 2015 | 3303 | 61 |
| 'Suzuki | VITARA | 2.0 | 3.1 | 0.2 | 6 | -16.4 | 1040 | 1365 | 76 |
| 'Saab | 9.3 | 1.8 | 3.1 | 0.4 | 14 | -7.2 | 736 | 1478 | 50 |
| 'Volkswagen | PASSAT | 1.8 | 3.1 | 0.6 | 20 | -5.1 | 1525 | 3501 | 44 |
| 'Ford | MONDEO | 2.0 | 3.1 | 0.6 | 19 | -5.2 | 1710 | 3239 | 53 |
| 'Peugeot | 407 | 1.6 | 3.0 | 0.5 | 17 | -9.9 | 355 | 953 | 37 |
| 'Audi | A4 | 1.6 | 3.0 | 0.3 | 10 | -15.3 | 639 | 2411 | 27 |
| Toyota | AVENSIS | 1.8 | 3.0 | 0.8 | 25 | -4.8 | 2049 | 6301 | 33 |
| 'Citroen | C5 | 1.8 | 2.9 | 0.2 | 6 | -22.6 | 341 | 968 | 35 |
| Volvo | V50 | 1.8 | 2.9 | 0.4 | 13 | -15.6 | 705 | 1247 | 57 |
| 'Opel | ZAFIRA | 1.8 | 2.8 | 0.7 | 26 | -3.9 | 360 | 885 | 41 |
| 'Opel | VECTRA | 1.8 | 2.8 | 0.5 | 19 | -5.4 | 1629 | 2996 | 54 |
| 'Renault | MEGANE | 1.6 | 2.5 | 0.6 | 25 | -4.4 | 595 | 1884 | 32 |
| 'Mazda | 6 | 1.8 | 2.5 | 0.2 | 20 | -13.6 | 994 | 2205 | 45 |
| 'Audi | A3 | 1.6 | 2.5 | 0.1 | 5 | -22.8 | 1009 | 1286 | 78 |
| 'Nissan | PRIMERA | 1.6 | 2.5 | 0.1 | 5 | -46.7 | 217 | 1025 | 21 |
| 'Renault | LAGUNA | 1.6 | 2.5 | 0.2 | 8 | -17.1 | 487 | 827 | 59 |
| 'Skoda | OCTAVIA | 1.8 | 2.5 2.5 | 0.2 | 13 | -17.1 | 547 | 1866 | 29 |
| 'Suzuki | LIANA | 1.6 | 2.0 2.4 | 0.6 | 25 | -5.1 | 1439 | 1446 | 100 |
| Volvo | S40 | 1.6 | 2.4 2.4 | 0.8 | 35 | -3.7 | 1455 | 1939 | 60 |
| 'Citroen | XSARA | 1.6 | 2.3 | 0.2 | 10 | -10.3 | 225 | 768 | 29 |
| Toyota | COROLLA | 1.6 | 2.3 | 0.2 | 25 | -4.4 | 1787 | 5205 | 34 |
| 'Ford | FOCUS | 1.6 | 2.3 | 0.0 | 23 14 | -4.4 | 917 | 2712 | 34 |
| 'Mitsubishi | LANCER | 1.6 | 2.3 | 0.3 | 6 | -22.8 | 372 | 609 | 61 |
| Volkswagen | GOLF | 1.6 | 2.3 | 0.1 | 6 | -19.5 | 2697 | 5662 | 48 |
| 'Peugeot | 307 | 1.6 | 2.3 | 0.1 | 22 | -19.5 | 1272 | 3002 4454 | 40 29 |
| 'Mazda | 3 | 1.6 | 2.2 | 0.5 | 3 | -4.0 -56.1 | 576 | 4434 841 | 29 68 |
| 'Opel | ASTRA | 1.6 | 2.2 2.1 | 0.1 | 10 | -10.4 | 576 731 | 1756 | 42 |
| - | | | | | 28 | -10.4 -3.7 | | | |
| 'Opel 'Suzulti | MERIVA IGNIS | 1.6 | $2.1 \\ 1.9$ | 0.6 | 28 12 | -3.7 -9.1 | 603 474 | 1107 932 | 54 51 |
| 'Suzuki 'Citroon | C3 | $1.4 \\ 1.4$ | 1.9 1.9 | 0.2 0.0 | 12 | -9.1 -51.1 | 474 254 | 932 623 | 51 41 |
| 'Citroen | | | | | 2 33 | | | | |
| 'Volkswagen | POLO | 1.2 | 1.8 | 0.6 | | -3.3 | 1483 | 1901 | 78 70 |
| 'Ford | FIESTA | 1.4 | 1.8 | 0.1 | 5 | -21.5 | 508 | 641 | 79 86 |
| 'Hyundai | GETZ | 1.4 | 1.6 | 0.2 | 9 | -11.1 | 1106 | 1284 | 86 |
| "Toyota | YARIS | 1.0 | 1.6 | 0.4 | 24 | -4.2 | 1363 | 2914 | 47 |
| 'Skoda | FABIA | 1.2 | 1.6 | 0.2 | 10 | -10.7 | 519 | 1106 | 47 |

TABLE 5 MARKUPS FOR BEST-SELLING PRODUCTS ORDERED BY PRICE

| | | | | | | | | 1 | ABLE | 0 | | | | | | | | | | | |
|------------------|-------|-------|-------|--------|------|-----|-------|------|-------|-----|-------|------|-------|------|-------|------|-------|------|-----|-----|-----|
| Modi | el Pr | ICE I | Elast | ICITIE | S OF | SAM | ple I | RODU | JCTS, | COM | IPUTE | D WI | TH AL | l Va | RIANT | s 90 | 4 Pro | ODUC | TS | | |
| Porsche 911 | -5 | 0.1 | 0.0 | 0.0 | 0.5 | 0.0 | 0.1 | 0.0 | 0.1 | 0.6 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Ast. Martin DB9 | 0.1 | -15 | 0.0 | 0.0 | 0.9 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Range Rover | 0.0 | 0.0 | -12 | 3.2 | 0.3 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| VW Touareg | 0.0 | 0.0 | 1.5 | -60 | 0.3 | 0.0 | 0.4 | 0.9 | 0.5 | 0.0 | 0.9 | 0.5 | 0.0 | 0.0 | 0.2 | 0.2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Audi A8 | 0.1 | 0.1 | 0.4 | 0.6 | -84 | 1.7 | 20 | 3.0 | 0.2 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Mercedes S-class | 0.0 | 0.0 | 0.0 | 0.0 | 4.5 | -88 | 0 | 0.1 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Mercedes E-class | 0.0 | 0.0 | 0.0 | 0.1 | 0.9 | 0.7 | -19 | 1.8 | 4.4 | 0.1 | 0.1 | 0.0 | 0.0 | 0.1 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| BMW 5-series | 0.0 | 0.0 | 0.0 | 0.2 | 0.3 | 0.0 | 2.9 | -34 | 4.6 | 0.3 | 0.1 | 0.1 | 0.4 | 0.0 | 0.1 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 |
| Audi A4 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.0 | 4.8 | 2.4 | -57 | 4.3 | 0.8 | 3.4 | 0.6 | 0.2 | 1.3 | 1.4 | 0.4 | 0.3 | 0.1 | 0.0 | 0.0 |
| BMW 3-series | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.2 | 0.3 | 11 | -34 | 0.8 | 4.7 | 1.0 | 0.0 | 3.1 | 3.9 | 0.6 | 0.0 | 0.0 | 0.0 | 0.0 |
| Ford Mondeo | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.7 | 0.2 | -43 | 1.7 | 0.3 | 0.9 | 1.1 | 0.3 | 0.9 | 0.0 | 0.0 | 0.0 | 0.0 |
| VW Passat | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 4.0 | 1.2 | 2.5 | -17 | 0.2 | 0.2 | 0.6 | 1.0 | 0.2 | 0.0 | 0.0 | 0.0 | 0.0 |
| Volvo S40 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.3 | 1.1 | 0.5 | 0.6 | 0.2 | -21 | 0.1 | 1.4 | 0.2 | 0.4 | 0.0 | 0.1 | 0.0 | 0.0 |
| Citron C5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.4 | 0.0 | 0.8 | 0.0 | 2.7 | 0.4 | 0.1 | -32 | 1.0 | 0.0 | 0.2 | 0.0 | 0.1 | 0.0 | 0.0 |
| Toyota Avensis | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.6 | 0.5 | 0.6 | 0.2 | 0.3 | 0.1 | -37 | 1.7 | 0.4 | 0.0 | 0.1 | 0.0 | 0.0 |
| VW Golf | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.9 | 0.8 | 0.4 | 0.5 | 0.1 | 0.0 | 4.1 | -27 | 2.6 | 0.3 | 0.8 | 0.0 | 0.0 |
| Opel Astra | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 1.0 | 0.5 | 2.2 | 0.2 | 0.4 | 0.1 | 2.3 | 6.8 | -71 | 0.3 | 0.8 | 0.0 | 0.0 |
| Toyota Yaris | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.8 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 1.2 | 0.3 | -12 | 0.3 | 0.0 | 0.0 |
| Peugeot 206 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.4 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 1.0 | 2.4 | 1.1 | 0.5 | -40 | 0.1 | 0.2 |
| Fiat Punto | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.2 | 0.1 | 0.4 | 3.7 | -14 | 1.0 |
| Daewoo Matiz | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1.3 | 0.3 | 0.0 | 4.0 | 0.6 | -42 |

TABLE 6

| MODEL | PRICE | E ELA | ASTICI | TIES | OF B | EST-S | ELLIN | IG PF | RODU | CTS, | Сомр | UTED | WITH | ALL | VARI | ANTS | 904 | PROI | DUCTS | <u> </u> | |
|-----------------|-------|-------|--------|------|------|-------|-------|-------|------|------|------|------|------|-----|------|------|-----|------|-------|----------|-----|
| Volvo V70 | -14 | 0.0 | 0.0 | 0.1 | 0.3 | 0.0 | 0.0 | 0.1 | 0.7 | 0.3 | 0.4 | 0.0 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Nissan X-Trail | 0.0 | -22 | 0.3 | 2.3 | 0.1 | 0.0 | 0.1 | 0.6 | 0.3 | 0.1 | 0.1 | 0.2 | 0.0 | 0.2 | 0.1 | 0.0 | 0.1 | 0.1 | 0.0 | 0.0 | 0.0 |
| Honda CR-V | 0.0 | 0.4 | -9 | 2.2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.3 | 1.0 | 0.1 | 0.0 | 0.1 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Toyota RAV4 | 0.1 | 2.2 | 1.6 | -12 | 0.1 | 0.0 | 0.0 | 0.0 | 0.4 | 1.0 | 0.2 | 0.3 | 0.0 | 0.0 | 0.0 | 0.1 | 0.1 | 0.1 | 0.0 | 0.0 | 0.0 |
| Subaru Forester | 0.6 | 0.1 | 0.0 | 0.2 | -15 | 0.0 | 0.0 | 0.0 | 2.6 | 0.1 | 0.0 | 0.1 | 0.3 | 0.3 | 0.0 | 0.0 | 0.8 | 0.1 | 0.0 | 0.0 | 0.0 |
| VW Touran | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | -12 | 0.1 | 0.1 | 0.8 | 1.2 | 0.3 | 0.2 | 0.0 | 0.1 | 0.1 | 0.2 | 0.2 | 0.6 | 0.7 | 0.0 | 0.0 |
| VW Passat | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.2 | -17 | 2.5 | 4.0 | 0.6 | 1.5 | 0.1 | 0.2 | 1.7 | 0.2 | 0.1 | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 |
| Ford Mondeo | 0.1 | 0.5 | 0.0 | 0.0 | 0.0 | 0.1 | 1.7 | -43 | 0.7 | 1.1 | 24 | 0.1 | 0.7 | 0.6 | 0.3 | 0.0 | 0.7 | 0.3 | 0.1 | 0.0 | 0.0 |
| Audi A4 | 0.8 | 0.2 | 0.2 | 0.4 | 1.3 | 0.9 | 3.4 | 0.8 | -57 | 1.3 | 1.1 | 0.1 | 0.2 | 1.1 | 0.6 | 0.7 | 0.8 | 1.4 | 0.2 | 0.0 | 0.3 |
| Toyota Avensis | 0.2 | 0.0 | 0.3 | 0.4 | 0.0 | 0.5 | 0.2 | 0.6 | 0.6 | -37 | 1.1 | 0.2 | 2.8 | 0.2 | 0.3 | 2.0 | 0.1 | 1.7 | 0.4 | 0.0 | 0.0 |
| Opel Vectra | 0.6 | 0.1 | 0.0 | 0.1 | 0.0 | 0.2 | 0.9 | 26 | 1.2 | 2.9 | -50 | 0.1 | 0.6 | 0.4 | 0.4 | 0.1 | 1.1 | 0.6 | 0.1 | 0.0 | 0.0 |
| Renault Megane | 0.0 | 0.3 | 0.0 | 0.5 | 0.1 | 0.6 | 0.1 | 0.2 | 0.3 | 1.2 | 0.1 | -56 | 0.1 | 0.8 | 0.2 | 0.3 | 1.7 | 2.2 | 18 | 0.2 | 0.0 |
| Mazda 6 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.3 | 1.8 | 0.4 | 11.2 | 1.5 | 0.1 | -29 | 0.4 | 0.1 | 0.1 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 |
| Skoda Octavia | 0.2 | 0.3 | 0.1 | 0.1 | 0.2 | 0.3 | 2.9 | 1.5 | 2.6 | 1.6 | 1.0 | 0.4 | 0.6 | -34 | 0.2 | 0.7 | 0.4 | 2.4 | 0.5 | 0.0 | 0.2 |
| Volvo S40 | 0.0 | 0.1 | 0.0 | 0.0 | 0.0 | 0.2 | 0.2 | 0.6 | 1.1 | 1.4 | 0.9 | 0.2 | 0.1 | 0.2 | -21 | 0.2 | 1.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| Toyota Corolla | 0.0 | 0.0 | 0.0 | 0.2 | 0.0 | 0.2 | 0.0 | 0.0 | 0.7 | 4.9 | 0.1 | 0.2 | 0.0 | 0.3 | 0.2 | -18 | 0.7 | 1.2 | 0.4 | 0.1 | 1.5 |
| Ford Focus | 0.0 | 0.1 | 0.0 | 0.1 | 0.6 | 0.3 | 0.0 | 0.7 | 1.3 | 0.4 | 1.2 | 0.9 | 0.0 | 0.5 | 0.6 | 0.5 | -30 | 0.1 | 0.1 | 0.0 | 0.2 |
| VW Golf | 0.0 | 0.1 | 0.0 | 0.1 | 0.0 | 0.7 | 0.5 | 0.4 | 0.9 | 4.1 | 0.5 | 1.1 | 0.0 | 1.1 | 0.1 | 0.6 | 0.1 | -27 | 0.2 | 0.6 | 0.3 |
| Peugeot 307 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.7 | 0.0 | 0.4 | 0.2 | 0.8 | 0.1 | 7.4 | 0.0 | 0.3 | 0.0 | 0.5 | 0.1 | 0.3 | -17 | 0.0 | 0.0 |
| VW Polo | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.2 | 0.0 | 0.0 | 0.2 | 0.1 | 0.0 | 0.4 | 0.0 | 0.1 | 0.0 | 0.1 | 0.1 | 2.8 | 0.1 | -12 | 0.4 |
| Toyota Yaris | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.1 | 0.0 | 0.0 | 0.8 | 0.1 | 0.0 | 0.0 | 0.0 | 0.2 | 0.0 | 3.1 | 0.3 | 1.2 | 0.0 | 0.2 | -12 |

 Table 7

 Model Price Elasticities of Best-Selling Products, Computed with all Variants 904 Products

| Pric | E EL | ASTIC | ITIES | OF S | SAMPL | e Pro | DUC | rs, C | OMPU | TED | WITH | Mod | al VA | ARIAN | rs Oi | NLY, | 199 I | PRODU | JCTS | | |
|------------------|------|-------|-------|-------|-------|-------|------|-------|-------|-------|------|------|-------|-------|-------|-------|-------|-------|------|-------|-------|
| Porsche 911 | -6.1 | 0.07 | 0.00 | 0.00 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Ast. Martin DB9 | 0.04 | -5.4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Range Rover | 0.00 | 0.00 | -6.4 | 1.28 | 0.13 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| VW Touareg | 0.00 | 0.00 | 0.34 | -12.0 | 0.27 | 0.02 | 0.51 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 |
| Audi A8 | 0.01 | 0.00 | 0.04 | 0.28 | -16.6 | 0.18 | 2.68 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Mercedes S-class | 0.00 | 0.00 | 0.00 | 0.07 | 1.60 | -51.5 | 23.7 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Mercedes E-class | 0.00 | 0.00 | 0.00 | 0.13 | 1.21 | 1.06 | -5.4 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| BMW 5-series | 0.00 | 0.00 | 0.00 | 0.02 | 0.03 | 0.00 | 0.03 | -3.2 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 |
| Audi A4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | -15.3 | 5.34 | 0.52 | 0.19 | 0.13 | 0.32 | 0.52 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| BMW 3-series | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 7.5 | -13.5 | 0.00 | 0.00 | 0.00 | 0.00 | 2.06 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Ford Mondeo | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.09 | 0.00 | -5.2 | 0.96 | 0.01 | 0.02 | 0.26 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| VW Passat | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.10 | 0.00 | 3.04 | -5.1 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Volvo S40 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.08 | 0.00 | 0.07 | 0.01 | -3.7 | 0.04 | 0.37 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Citron C5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.48 | 0.00 | 0.20 | 0.00 | 0.10 | -22.6 | 0.83 | 0.00 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 |
| Toyota Avensis | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.09 | 0.24 | 0.25 | 0.00 | 0.07 | 0.09 | -4.8 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 |
| VW Golf | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.03 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | -19.5 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 |
| Opel Astra | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.04 | 0.10 | -10.3 | 0.04 | 0.00 | 0.00 | 0.00 |
| Toyota Yaris | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.06 | -4.2 | 0.15 | 0.01 | 0.00 |
| Peugeot 206 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.01 | 0.36 | -6.7 | 0.23 | 0.30 |
| Fiat Punto | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 0.00 | 0.01 | 0.00 | 0.25 | 1.66 | -11.9 | 0.69 |
| Daewoo Matiz | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.80 | 0.27 | -12.3 |

 Table 8

 CE Elasticities of Sample Products, Computed with Modal Variants Only 199 Product

| TABLE S | • |
|---------|---|
|---------|---|

| Pri | CE EI | LASTIC | CITIES | OF | BEST-S | ELLIN | ig Pr | ODUC | ts, Co | OMPU | TED V | VITH 1 | Modai | L VA | RIANTS | 6 Oni | X, 19 | 9 Pro | DUCT | s | |
|--------------|-------|--------|--------|------|--------|--------|-----------|---------|--------|------|-------|--------|-------|--------------|--------|----------|-------|-------|------|-------|------|
| Volvo V70 | -5.8 | 0.10 | 0.08 | 0.06 | 0.17 | 0.00 | 0.00 | 0.32 | 0.00 | 0.04 | 0.00 | 0.00 | 0.00 | 0.21 | 0.00 | 0.01 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 |
| Nissan | 0.16 | -9.0 | 0.05 | 0.92 | 0.00 | 0.05 | 0.00 | 0.60 | 0.00 | 0.05 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| X-Trail | | | | | | | | | | | | | | | | | | | | | |
| Honda CR-V | 0.09 | 0.04 | -3.0 | 0.05 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.05 | 0.00 | 0.00 | 0.01 | 0.04 | 0.00 | 0.04 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 |
| Toyota | 0.20 | 1.64 | 0.12 | -8.5 | 0.00 | 0.02 | 0.00 | 0.11 | 0.00 | 0.07 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| RAV4 | | | | | | | | | | | | | | | | | | | | | |
| Subaru | 0.61 | 0.00 | 0.03 | 0.00 | -10.6 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.08 | 0.00 | 0.00 | 0.77 | 0.00 | 0.00 | 0.00 | 0.00 |
| Forester | | | | | | | | | | | | | | | | | | | | | |
| VW Touran | 0.00 | 0.05 | 0.00 | 0.02 | 0.00 | -3.9 | 0.09 | 0.14 | 0.01 | 0.05 | 0.01 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.02 | 0.00 |
| VW Passat | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.16 | -5.1 | 3.04 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.64 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Ford | 0.32 | 0.34 | 0.00 | 0.04 | 0.00 | 0.09 | 0.96 | -5.2 | 0.09 | 0.26 | 0.44 | 0.00 | 0.07 | 0.16 | 0.01 | 0.00 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 |
| Mondeo | | | | | | | | | | | | | | | | | | | | | |
| Audi A4 | 0.01 | 0.00 | 0.00 | 0.00 | 0.01 | 0.04 | 0.19 | 0.52 | -15.3 | 0.52 | 0.50 | 0.00 | 0.18 | 0.02 | 0.13 | 0.00 | 0.02 | 0.10 | 0.00 | 0.00 | 0.00 |
| Toyota | 0.04 | 0.03 | 0.04 | 0.02 | 0.00 | 0.03 | 0.00 | 0.25 | 0.09 | -4.8 | 0.26 | 0.02 | 0.83 | 0.01 | 0.07 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 |
| Avensis | | | | | | | | | | | | | | | | | | | | | |
| Opel Vectra | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 1.02 | 0.20 | 0.70 | -5.4 | 0.01 | 0.05 | 0.00 | 0.07 | 0.00 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 |
| Renault | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 0.03 | 0.00 | 0.18 | 0.04 | -4.4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.09 | 0.00 | 0.00 |
| Megane | | | | | | | | | | | | | | | | | | | | | |
| Mazda 6 | 0.00 | 0.00 | 0.02 | 0.00 | 0.00 | 0.02 | 0.00 | 0.26 | 0.13 | 3.84 | 0.13 | 0.00 | -13.6 | 0.04 | 0.02 | 0.00 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 |
| Skoda | 0.87 | 0.01 | 0.08 | 0.06 | 0.14 | 0.02 | 0.70 | 0.61 | 0.01 | 0.04 | 0.00 | 0.00 | 0.04 | -7.8 | 0.01 | 0.07 | 0.79 | 0.00 | 0.00 | 0.00 | 0.00 |
| Octavia | | | | | | | | | | | | | | | | | | | | | |
| Volvo S40 | | | 0.00 | | | | | 0.0.000 | | | | | 0.02 | 0505050000 | | | | 0.00 | | | |
| Toyota | 0.03 | 0.00 | 0.08 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 | 0.07 | 0.00 | -4.4 | 0.01 | 0.00 | 0.00 | 0.09 | 0.68 |
| Corolla | | | | | | | | | | | | | | | | | | | | | |
| Ford Focus | | | 0.03 | | 1.13 | | | | | | | | 0.01 | | | | | | | | |
| VW Golf | | | 0.00 | | | | | 0.00 | | | | 0.00 | | | | | | -19.5 | | | |
| | | | 0.00 | | | 205 G. | a.c.a. a. | 0.00 | | | | 0.05 | | 1.201.201.20 | | 0.000.00 | 0.00 | 0.01 | | 0.000 | |
| VW Polo | | | 0.00 | | | | | 0.00 | | | | 0.00 | 0.00 | | | | | 0.03 | | | |
| Toyota Yaris | 0.01 | 0.00 | 0.02 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 1.26 | 0.01 | 0.00 | 0.00 | 0.00 | -4.2 |

215

products.

In Table 7 the belt around the diagonal is much thicker. The products in this matrix are the best selling cars, and are located at the centre of characteristics space, which is where they appeal to the largest number of consumers. These products are therefore closer substitutes than those in the previous table, which included the models at the fringes of characteristics space. Accordingly, cross elasticities are positive for almost all products. It is still true, however, that elasticities are lower the further away they are from the diagonal.

Overall, the substitution patterns resulting from method I seem very reasonable, although the magnitudes of the substitution effects are high. Bajari and Benkard (2005) also find large price elasticities in their application to demand for personal computers. They suggest that the result is due to the assumption of perfect information about all products on the part of consumers, and conclude that this is unlikely to hold with a choice set containing 700 products. To mitigate this problem they remove from the choice set any product with a market share of less than 0.75%. This left them with only 24 products, and median own price elasticity fell from -100 to -11. In a similar way I remove all but the modal (bestselling) variants of each model, the choice set becomes the same as that used by Berry, Levinsohn, and Pakes (1995). All models are still included. The last column of Table 5 shows that the modal variant usually represents a very large proportion of the total sales of the model. I also tried to remove all models with market shares of less than 0.5%, leaving 40 products. This gave a median own price elasticity of -5, but this market share threshold is of course somewhat arbitrary.

As expected, elasticities are much lower with method II. This also means that many more cross elasticities are zero. In Table 8, the belt of positive cross elasticities around the diagonal is much narrower than in Table 6. Removing all but the modal variant of each model removes a model from areas of characteristics space which it does in fact cover, but which are not covered by the modal variant. In these areas of characteristics space it may be close neighbours with other models whose modal variants are quite different from its own modal variant. In this way, products which are in fact substitutes in variant-space (which is what the consumer faces) are not in model-space. The general features of the substitution patterns remain unchanged when moving from method I to method II.

In table 8, products in the middle of the matrix have more substitutes than the ones on the fringes, and the high selling products in

216

A PURE CHARACTERISTICS DEMAND MODEL

TABLE 10

CLOSEST SUBSTITUTES FOR FOUR SAMPLE PRODUCTS, COMPUTED USING HIGHEST CROSS-ELASTICITIES W.R.T. THE SAMPLE PRODUCTS, WHEN CHOICE SET HAS MODAL VARIANT ONLY

| | CHOICE SE | et has Mo | dal Varia | NT ONLY | |
|-------------|-----------|-----------|-----------|---------|-------------|
| Make | Model | ltr | m | pri | Bodytype |
| Volkswagen | GOLF | 1.6 | 4.2 | 2.3 | hatchback |
| 'Bmw | 1 | 1.6 | 4.2 | 2.5 | hatchback |
| 'Audi | A3 | 1.6 | 4.2 | 2.5 | hatchback |
| 'Kia | CERATO | 1.6 | 4.4 | 2.2 | hatchback |
| 'Daewoo | KALOS | 1.2 | 3.8 | 1.3 | hatchback |
| 'Subaru | JUSTY | 1.4 | 3.8 | 2.0 | hatchback |
| 'Daewoo | LACETTI | 1.4 | 4.4 | 1.6 | hatchback |
| 'Audi | A2 | 1.4 | 3.8 | 2.3 | MPV/minivan |
| 'Subaru | IMPREZA | 1.6 | 4.4 | 2.5 | station |
| 'Skoda | FABIA | 1.2 | 4.2 | 1.6 | station |
| 'Volvo | V50 | 1.8 | 4.6 | 2.9 | station |
| Toyota | AVENSIS | 1.8 | 4.8 | 3.0 | station |
| 'Mazda | 6 | 1.8 | 4.8 | 2.5 | station |
| 'Fiat | STILO | 1.6 | 4.6 | 2.1 | station |
| 'Mitsubishi | LANCER | 1.6 | 4.4 | 2.3 | station |
| 'Bmw | 3 | 1.8 | 4.4 | 3.2 | station |
| 'Nissan | 350Z | 3.4 | 4.4 | 7.9 | coup |
| 'Volvo | V50 | 1.8 | 4.6 | 2.9 | station |
| 'Audi | A6 | 1.8 | 4.8 | 4.4 | station |
| 'Kia | CERATO | 1.6 | 4.4 | 2.2 | hatchback |
| 'Kia | CARENS | 1.6 | 4.4 | 2.1 | MPV/minivan |
| 'Citroen | C5 | 1.8 | 4.8 | 2.9 | station |
| Ford | FOCUS | 1.6 | 4.4 | 2.3 | station |
| 'Mitsubishi | SPACE | 1.6 | 4 | 2.2 | station |
| 'Chrysler | PT | 1.6 | 4.2 | 2.6 | station |
| 'Opel | AGILA | 1 | 3.6 | 1.5 | station |
| 'Hyundai | ACCENT | 1.4 | 4.2 | 1.7 | hatchback |
| 'Skoda | OCTAVIA | 1.8 | 4.6 | 2.5 | station |
| 'Subaru | FORESTER | 2 | 4.4 | 3.4 | station |
| 'Subaru | LEGACY | 2 | 4.8 | 3.5 | station |
| 'Hyundai | ATOS | 1 | 3.6 | 1.3 | hatchback |
| 'Opel | MERIVA | 1.6 | 4 | 2.1 | MPV/minivan |
| 'Ford | FIESTA | 1.4 | 4 | 1.8 | hatchback |
| Audi | A4 | 1.6 | 4.6 | 3.0 | station |
| 'Bmw | 3 | 1.8 | 4.4 | 3.2 | station |
| 'Volkswagen | CADDY | 1.4 | 4.4 | 2.1 | station |
| 'Daewoo | NUBIRA | 1.6 | 4.6 | 2.0 | station |
| 'Fiat | STILO | 1.6 | 4.6 | 2.1 | station |
| 'Fiat | MAREA | 1.6 | 4.4 | 2.2 | station |
| 'Audi | A3 | 1.6 | 4.2 | 2.5 | hatchback |
| 'Volvo | V50 | 1.8 | 4.6 | 2.9 | station |
| 'Skoda | FABIA | 1.2 | 4.2 | 1.6 | station |
| 'Fiat | DOBLO | 1.6 | 4.2 | 2.1 | station |
| 'Audi | A2 | 1.4 | 3.8 | 2.3 | MPV/minivan |
| | | | | | |

TABLE 11

| CLOSEST SUBSTITUTES FOR FOUR SAMPLE PRODUCTS, COMPUTED USING |
|--|
| HIGHEST CROSS-ELASTICITIES W.R.T. THE SAMPLE PRODUCTS, WHEN |
| CHOICE SET HAS ALL VARIANTS |

| | CHOICE SET | HAS AL | L VARIANT | s | |
|----------------|------------|--------------|------------|-------------------|--------------|
| Make | Model | ltr | m | pri | Bodytype |
| Volkswagen | GOLF | 1.6 | 4.2 | 2.3 | hatchback |
| 'Kia | CERATO | 1.6 | 4.4 | 2.2 | hatchback |
| 'Daewoo | LACETTI | 1.4 | 4.4 | 1.6 | hatchback |
| 'Daewoo | KALOS | 1.2 | 3.8 | 1.3 | hatchback |
| 'Bmw | 1 | 1.6 | 4.2 | 2.5 | hatchback |
| 'Fiat | STILO | 1.6 | 4.6 | 2.1 | station |
| 'Audi | A3 | 1.6 | 4.2 | 2.5 | hatchback |
| 'Volkswagen | CADDY | 1.4 | 4.4 | 2.1 | station |
| 'Audi | A2 | 1.4 | 3.8 | 2.3 | MPV/minivan |
| 'Opel | ASTRA | 1.6 | 4.2 | 2.0 2.1 | hatchback |
| 'Jeep | WRANGLER | 2.4 | 3.8 | 3.9 | Off-road/SUV |
| | | | | | |
| Toyota | AVENSIS | 1.8 | 4.8 | 3.0 | station |
| 'Mazda | 3 | 1.6 | 4.4 | 2.2 | hatchback |
| 'Mitsubishi | CARISMA | 1.6 | 4.4 | 2.3 | hatchback |
| 'Kia | CERATO | 1.6 | 4.4 | 2.2 | hatchback |
| 'Fiat | STILO | 1.6 | 4.6 | 2.1 | station |
| 'Nissan | 350Z | 3.4 | 4.4 | 7.9 | coup |
| 'Mitsubishi | LANCER | 1.6 | 4.4 | 2.3 | station |
| 'Alfa Romeo | 156 | 1.8 | 4.4 | 3.0 | sedan |
| 'Renault | LAGUNA | 1.6 | 4.8 | 2.5 | station |
| 'Honda | CIVIC | 1.6 | 4.2 | 2.3 | hatchback |
| 'Mazda | 6 | 1.8 | 4.8 | 2.5 | station |
| Ford | FOCUS | 1.6 | 4.4 | 2.3 | station |
| 'Fiat | MAREA | 1.6 | 4.4 | 2.2 | station |
| 'Alfa Romeo | 147 | 1.6 | 4.2 | 2.6 | hatchback |
| 'Chrysler | РТ | 1.6 | 4.2 | 2.6 | station |
| 'Nissan | PATROL | 3 | 5 | 7.1 | Off-road/SUV |
| 'Opel | ASTRA | 1.6 | 4.2 | 2.1 | hatchback |
| 'Opel | AGILA | 1.0 | 3.6 | 1.5 | station |
| 'Ford | FUSION | 1.4 | 4 | 2.0 | MPV/minivan |
| 'Ford | FIESTA | $1.4 \\ 1.4$ | 4 | 1.8 | hatchback |
| 'Seat | LEON | 1.4 | 4.2 | $1.0 \\ 2.1$ | hatchback |
| 'Nissan | MICRA | $1.0 \\ 1.2$ | 4.2 3.8 | $\frac{2.1}{1.7}$ | hatchback |
| | | | | | |
| Audi | A4 | 1.6 | 4.6 | 3.0 | station |
| 'Alfa Romeo | 166 | 2 | 4.8 | 4.5 | sedan |
| 'Nissan | PATROL | 3 | 5 | 7.1 | Off-road/SUV |
| 'Jeep | WRANGLER | 2.4 | 3.8 | 3.9 | Off-road/SUV |
| 'Bmw | 3 | 1.8 | 4.4 | 3.2 | station |
| 'Volkswagen | BORA | 1.6 | 4.4 | 2.5 | sedan |
| 'Volkswagen | CADDY | 1.4 | 4.4 | 2.1 | station |
| 'Seat | TOLEDO | 1.6 | 4.4 | 2.3 | sed |
| 'Bmw | 5 | 2.2 | 4.8 | 4.7 | sedan |
| 'Mercedes-Benz | Č | 1.8 | 4.6 | 3.7 | sedan |
| 'Mercedes-Benz | E | 2.2 | 4.8 | 5.4 | sedan |
| | | | | 5.1 | |

Table 9 have many more substitutes than the ones in Table 8. The size of the elasticities is now much more reasonable, with all but three of the own elasticities being single digit for the top selling products. It appears that low market share products are more likely to have particularly large elasticities, such as the Mercedes S-class in Table 8, with -51. This is possibly because revealed preference conditions constrain taste parameters less for special (low market share) products than for products in the more densely populated parts of characteristics space, leading to bad estimates of these consumers' preferences. For the higher-selling products, elasticities largely appear reasonable. Some examples of seemingly reasonable high cross elasticities between similar products are the two SUVs, Range Rover and VW Touareg (1.28 and 0.34) or Ford Mondeo and VW Passat (0.96 and 3.04).

Table 10 shows the ten best substitutes for four randomly chosen highselling products in a densely populated area of characteristics space. The substitutes are ranked according to their elasticities with respect to the price of the sample car. (I also tried to rank substitutes using derivatives or displacement ratios, but this did not make much of a difference.) To the left are best substitutes for one-variant case and to the right is the many-variants case. The number of substitutes that are common to the two cases is 6 out of 10 for the VW Golf, 5 for the Toyota Avensis, 3 for the Ford Focus, and 2 for the Audi A4. As expected, the inclusion of all variants appears to make a difference.

D. Discussion

The method of this paper could be useful for other markets where consumers face a large number of alternatives, such as housing. See Hong (2013) and Cho and Kim (2013) for other approaches.

The data used in this paper are of a particularly simple form: one cross section, where the unit of observation is a product, and no consumerlevel information. It is therefore natural to ask what use could be made of more detailed data, such as several time periods or markets, and/or demographic information such as age, sex or income of consumers.

The method used in this paper can easily be adapted to obtain estimates of taste distributions in separate demographic groups, by simply replacing the market shares in equation (18) with the corresponding within-demographic-group market shares. In combination with the extensions for multiple time periods discussed below, this approach could be valuable for out-of-sample prediction exercises where demographics vary.

Data from multiple markets or time periods could potentially be used to tighten the bounds obtained in this paper, or to obtain information about the distribution of tastes within each A-set (the set of taste vectors which would rationalise the purchase of a given product).

If we consider the revealed preference conditions given in equation (7), it might be tempting to simply add to the system inequalities from multiple years of data. Such a straightforward approach is not consistent, however. Since the set of alternatives available presumably varies between years, the revealed preference inequalities for two different years are not statements about the same group of consumers. In principle, the set of taste vectors simultaneously satisfying the revealed preference conditions for two different years could even be empty.¹¹

A more promising approach is to estimate the distribution of consumer tastes in each year separately, as done in this paper, and then pool all the draws obtained, and use the resulting distribution as the estimated distribution of tastes, assuming that tastes in the population are constant across the years. The drawback is that we would not get a perfect fit to the data in any given year. The advantage, presumably, would be a better ability to predict out of sample.

VII. Conclusion

I estimate a modified version of a model developed in Bajari and Benkard (2005). The model has several advantages over the standard Berry, Levinsohn, and Pakes (1995) (BLP) model. It can be estimated with data from one time period and one market, unlike BLP which requires many markets for identification. It can also accommodate products with a larger number of characteristics than what is possible in BLP. I used 30. BLP assumes that taste coefficients are independently normally distributed. The Bajari-Benkard model makes no parametric assumptions on the taste distributions, and allows for dependence between the distributions. In BLP, simulation error becomes a problem when the number of products is very large (Berry, Linton, and Pakes 2004). In the Bajari-Benkard model, a large number of products is an advantage for the estimation of taste distributions.

(Received 10 September 2013; Revised 10 December 2013; Accepted 14 December 2013)

¹¹ An example showing this can easily be constructed for the simple vertical differentiation model set out in subsection III.A.

220

References

- Ackerberg, D. A., and M. Rysman. "Unobserved Product Differentiation in Discrete Choice Models: Estimating Price Elasticities and Welfare Effects." *RAND Journal of Economics* 36 (No. 4 2005): 771-88.
- Azzalini, A. "A Note on the Estimation of a Distribution Function and Quantiles by a Kernel Method." *Biometrika* 68 (No. 1 1981): 326-8.
- Bajari, P., and C. L. Benkard. Discrete Choice Models as Structural Models of Demand: Some Economic Implications of Common Approaches, Unpublished manuscript, Stanford University, 2003.
 - _____. "Demand Estimation With Heterogenous Consumers and Unobserved Product Characteristics: A Hedonic Approach." *Journal* of *Political Economy* 113 (No. 6 2005): 1239-76.
- Berry, S., J. Levinsohn, and A. Pakes. "Automobile Prices in Market Equilibrium." *Econometrica* 63 (No. 4 1995): 841-90.
- Berry, S., O. B. Linton, and A. Pakes. "Limit Theorems for Estimating the Parameters of Differentiated Products Demand Systems." *Review of Economic Studies* 71 (No. 3 2004): 613-54.
- Berry, S., and A. Pakes. "The Pure Characteristics Discrete Choice Model of Demand." *International Review of Economics* 48 (No. 4 2007): 1193-225.
- Blow, L., M. Browning, and I. Crawford. "Revealed Preference Analysis of Characteristics Models." *Review of Economic Studies* 75 (No. 2 2008): 371-89.
- Bresnahan, T. "Competition and Collusion in the American Automobile Oligopoly: The 1955 Price War." *Journal of Industrial Economics* 35 (No. 4 1987): 457-82.
- Caplin, A., and B. Nalebuff. "Aggregation and Imperfect Competition: On the Existence of Equilibrium." *Econometrica* 59 (No. 1 1991): 25-59.
- Cho, S. J., and J. R. Kim. "Housing and the Business Cycle: Evidence from the UK Housing Price and Quantity." Seoul Journal of Economics 26 (No. 4 2013): 383-400.
- Herceg, M., M. Kvasnica, C. Jones, and M. Morari. "Multi-Parametric Toolbox 3.0." In Proc. of the European Control Conference, pp. 502-510, Zürich, Available at: Switzerland. http://control.ee.ethz. ch/~mpt, No. EPFL-CONF-186265, 2013.
- Hong, E. P. "The Effect of a Special Interest Group on Apartment Price Collusion." Seoul Journal of Economics 26 (No. 3 2013): 337-60.

- Manski, C. F. "Analog Estimation of Econometric Models." In R. F. Engle, and D. L. McFadden (eds.), *Handbook of Econometrics*, Chapter 43, vol. 4, Netherlands: Elsevier, 1994.
- Martinez, W. L., and A. R. *Martinez Computational Statistics Handbook with MATLAB.* Florida: Chapman & Hall/CRC, 2002.
- Matzkin, R. L. "Nonparametric Estimation of Nonadditive Random Functions." *Econometrica* 71 (No. 5 2003): 1339-75.
- Mussa, M., and S. Rosen. "Monopoly and Product Quality." *Journal of Economic Theory* 18 (No. 2 1978): 301-17.
- Nadaraya, E. A. "Some New Estimates for Distribution Functions." *Theory* of *Probability and Its Applications*, 9 (No. 3 1964): 497-500.
- Nevo, A. "Measuring Market Power in the Ready-to-Eat Cereal Industry." *Econometrica* 69 (No. 2 2001): 307-42.
- Petrin, A. "Quantifying the Benefits of New Products: The Case of the Minivan." *Journal of Political Economy* 110 (No. 4 2002): 705-29.
- Robert, C. P., and G. Casella. Monte Carlo Statistical Methods, New York: Springer Texts in Statistics. Springer Science, second edition, 2004.
- Shaked, A., and J. Sutton. "Relaxing Price Competition Through Product Differentiation." *Review of Economic Studies* 49 (No. 1 1982): 3-13.